

Calculating the Ebb and Flow of Tides for Maui

February 12th, 2016, high tide occurred at 7:02 pm. At that time the water was 1.5 meters deep. Low tide occurred at 12:36 p.m, at which time the water was only .2 meters deep. Assume that the depth of the water is a sinusoidal function of time with a period of half a lunar day (about 12 hrs 24 min)

$$12.6$$

$$\frac{24}{60} = .6$$

$$\frac{2}{60} = .03$$

$$\frac{24}{60} = .4$$

$$12.4 \text{ hrs}$$

- a) Model the depth, D, as a sinusoidal function of time, t, algebraically then graph the function.

$$A = \frac{\text{max} - \text{min}}{2}$$

$$= \frac{1.5 - .2}{2} = \frac{1.3}{2} = .65$$

$$B = \frac{2\pi}{\text{Per}} = \frac{2\pi}{12.4} = \frac{\pi}{6.2}$$

Low tide

$$Y = -.65 \cos \frac{\pi}{6.2}(x - 12.6) + .85$$

$$D = \frac{\text{max} + \text{min}}{2} = \frac{1.5 + .2}{2}$$

$$\frac{1.7}{2} = .85$$

high tide

$$Y = .65 \cos \frac{\pi}{6.2}(x - 19.03) + .85$$

- b) At what time did the first low tide occur? $(.2)(60) = 12$
 $x = .19$ 12:12 am

- c) What was the approximate depth of the water at 6:00 am and at 3:00 pm?

$$6:00 \text{ am } \text{Let } x = 6 = 1.487 \text{ m}$$

$$3:00 \text{ pm } \text{Let } x = 15 = .62 \text{ m}$$

- d) What was the first time on this day when the water was 1 meter deep?

$$3.76$$

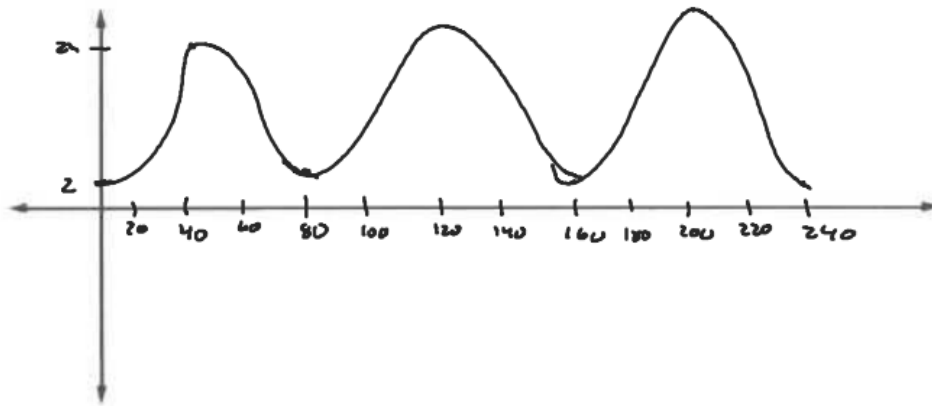
$$3:46 \text{ am}$$

The center of a Ferris wheel is 12 meters above the ground. The Ferris wheel itself has a diameter of ~~20~~²⁰ meters. The wheel turns counterclockwise at a constant rate and takes 80 seconds to make one complete revolution.

$$Y = -10 \cos \frac{\pi}{40} X + 12$$

$$\begin{array}{c} 22 \\ | \\ 10 \\ | \\ 12 \end{array}$$

- a. Suppose Jim and his friends enter a seat directly below the center of the Ferris Wheel. Sketch a graph that you would expect to show their height above the ground during a four-minute ride. Label the x-axis of your sketch using seconds. Label the y-axis using meters.



- b. What is the maximum height of the Ferris wheel? Minimum height?
- c. Write the equation to model path of the Ferris wheel.

